

# Structuring The Urban Airspace For Efficient Logistics Traffic Operation

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## Structuring The Urban Airspace For Efficient Logistics Traffic Operation

**Abstract:** This paper considers the problem of structuring the urban airspace so that UAVs-based-urban-logistics can be performed efficiently. This problem is important to guarantee mobility and accessibility for all operators. First, a set of assumptions about the organization of the lower layers of the urban airspace is proposed, then an optimal flow assignment problem is formulated, a heuristic solution approach is developed and, finally, its application to a medium size problem is displayed.

**Keywords:** UAVs; logistics; urban airspace; air traffic management; networks; optimization and heuristics.

## Estructuración del espacio aéreo urbano para un funcionamiento eficaz del tráfico logístico

**Resumen:** este trabajo considera el problema de la estructuración del espacio aéreo urbano para que la logística urbana basada en UAVs pueda realizarse de forma eficiente. Este problema es importante para garantizar la movilidad y accesibilidad de todos los operadores. En primer lugar, se propone un conjunto de hipótesis sobre la organización de las capas inferiores del espacio aéreo urbano, a continuación se formula un problema de asignación óptima de flujos, se desarrolla un enfoque heurístico de solución y, por último, se muestra su aplicación a un problema de tamaño medio.

**Palabras clave:** UAVs; logística; espacio aéreo urbano; gestión del tráfico aéreo; redes; optimización y heurística.

## Estruturação do espaço aéreo urbano para uma operação eficiente do tráfego logístico

**Resumo:** Este artigo considera o problema da estruturação do espaço aéreo urbano para que a logística urbana baseada em VANTs possa ser realizada de forma eficiente. Esse problema é importante para garantir a mobilidade e a acessibilidade de todos os operadores. Primeiro, é proposto um conjunto de suposições sobre a organização das camadas inferiores do espaço aéreo urbano, depois é formulado um problema de atribuição de fluxo ideal, é desenvolvida uma abordagem de solução heurística e, por fim, é apresentada sua aplicação a um problema de médio porte.

**Palavras-chave:** UAVs; logística; espaço aéreo urbano; gerenciamento de tráfego aéreo; redes; otimização e heurística.

## Introduction

UAV networks have been considered in the recent literature and are mainly related to either mobile communication networks, based on fleets of UAVs or with route generation for delivery services with UAVs. Important perspectives for the development of urban logistics based on the operation of UAVs have been consolidating, according to recent publications (Sah et al., 2021; Eun et al., 2019; Goodchild & Toy, 2018; Park et al., 2018; Koiwanit, 2018). These perspectives will be able to profit from the until now unused urban airspace to then alleviate ground traffic by diminishing the needs for ground-based logistic transportation, which is one of the main contributors to ground urban traffic congestion and pollution.

Previously, many studies have been devoted to the design of efficient UAVs based-urban-logistics systems (Roca-Riu & Menendez, 2019; Iranmanesh et al., 2020; Zubin et al., 2020), where, in general, traffic volumes and capacities are not taken as issues. However, Doole et al. (2018) show that, in few decades, the expected high traffic of drones operating in the urban airspace will make imperative its effective organization to turn feasible air traffic management. Structuring the airspace and adopting systematic procedures to operate this structured airspace will provide *ad-hoc* solutions for urban logistics air traffic operations (EmbraerX et al., n.d.). Then, the Air Traffic Management (EmbraerX, 2019) will be mainly in charge of flow management and dynamic airspace management.

In this study, the development of a method to structure the considered layer through the definition of a network of air links to operate traffic flows of UAVs devoted to general logistics in an urban area. This is considered through the resolution of the assignment of expected demand along feasible paths.

The paper is organized as follows: First, assumptions about operational objectives for UAVs-based-logistics in the urban airspace are proposed, leading to a structuring proposal for the lower layer of the urban airspace. Then, the optimization problem of the operated network inside the urban airspace is formulated

and a heuristic solution approach is developed and illustrated. Finally, the usefulness of this tool for Air Traffic Management is discussed.

## Basic assumptions and definitions

A basic assumption of this study is that urban logistic air traffic operates over the ground links of the considered urban area (avenues, streets and squares), while the urban passenger traffic is performed between the top of buildings (public and private) and open areas such as parks, cemeteries and outdoor parking areas. Then, it is considered that urban passenger air traffic is completely segregated from logistics air traffic, avoiding collision risks with those UAVs devoted to logistics. The urban area is supposed to be subdivided in subareas for which estimated or online origin-destination demand data is available. The considered air traffic flows are either local flows within a subarea or flows between subareas. A gate-to-gate flight between different subareas will present also an initial and a final local part.

The decision problem considered in this study is relative to the design of the urban airspace devoted to logistics flights between different subareas. This design is materialized through network linking reference points of the different subareas of the urban space. Once the network has been defined, users demand for air mobility will be assigned to paths belonging to this frame.

While designing this network, the main considered design objectives are to ensure mobility, accessibility and safety, master traffic safety, network capacity, and environmental impacts. The main constraints to be taken into consideration are the following:

- The designed network should provide reachability for any origin-destination pair associated with a demand for logistic UAVs services between subareas.

- The designed network is a capacitated network where each link is characterized by its length and capacity. This capacity is the maximum flow per unit of time compatible with a safety and local environmental impact.

As demand evolves in the short term (from one hour to another), the proposed solution must be easily adaptable to new demand profiles.

Let's then define the following sets, variables and parameters:

- $O$ , the set of origins, and  $D$ , the set of destinations, with in general  $|O| \ll |D|$ .
- $G$ : the oriented graph linking origins and destinations;
- $C_{hl}$ : the maximum air traffic allowed in airlink  $(h,l)$  during the considered period;
- $D_{ij}$ : the flight demand for airborne logistics between origin  $i$  and destination  $j$  during the considered period.

## Analysis of candidate problem formulations

The objective here is to determine which links will be used to realize the expected airborne logistics and what will be their intensity, considering some practical capacity attached to each candidate link. For this, a flow optimization problem is considered where the goal is to minimize the overall travelled distance while performing the airborne logistics operation. The considered problem presents specific characteristics when compared to traditional urban ground transportation network design problems or when it refers to air transportation network design problems, so new solution approaches should be developed.

The overall capacity  $C_G$  of the considered network can be computed using some of Ford & Fulkerson's scheme (1956) once a global source is connected to all the origins and a global sink is connected from all the destinations, both with infinite capacity links. A necessary condition for the feasibility of the flow assignment problem is that:

$$\sum_{i \in O} \sum_{j \in D} D_{ij} \leq C_G \quad (1)$$

A linear programming minimum cost flow problem can be easily formulated considering the minimization of total travelled distance under restrictions of positiveness, origin, destination, flow conservation, and capacity restrictions. However, when referring to the task of the traffic manager and the adopted point to point logistics operation, the decision variables are the paths adopted between each origin destination pair and their frequency. Then traffic flows in the urban network are the result of these traffic management decisions.

Taking as a basis the underlying street network and its local characteristics (overflight authorized or not), for each origin-destination pair a reduced set of possible air-paths linking them can be defined. Here it is also supposed that in a round trip the same path is used in reverse to come back to the origin of the flight.

The path flowbased-formulation of the design problem associated to the routing and capacity air-space management function of the Air Traffic Manager results in the following optimization problem:

$$\min \sum_{i \in O} \sum_{j \in D} \sum_{k \in P_{ij}^k} L_{ij}^k \cdot x_{ij}^k \quad (2)$$

under the constraints of capacity of the candidate elementary airlinks:

$$\sum_{i \in O} \sum_{j \in D} \sum_{k \in P_{ij}^k} a^{khl} \cdot x_{ij}^k \leq C_{h,l} \quad \forall (h,l), h \neq l \quad (3)$$

and

$$\sum_{k \in P_{ij}^k} x_{ij}^k = D_{ij} \quad \forall i, j, i \in O, j \in D \quad (4)$$

with

$$x_{ij}^k \geq 0 \quad k \in P_{ij}^k, \quad \forall i, j, i \in O, j \in D \quad (5)$$

where:

- $P_{ij}^k$  is the set of the  $K$  best elementary paths linking the origin  $i$  and the destination  $j$  in the air

logistic network of graph, where  $K$  is a small integer number;

- $U_{ij}^k$  is the set of elementary airlinks composing the  $k^{\text{th}}$  path between origin  $i$  and destination  $j$ ;
- $L_{ij}^k$  is the length of the  $k^{\text{th}}$  path between origin  $i$  and destination  $j$ :

$$L_{ij}^k = \sum_{(h,l) \in U_{ij}^k} L_{hl} \quad (6)$$

where  $L_{hl}$  is the length of airlink  $(h,l)$ ;

- $[a_{ij}^{khl}]$  is the incidence matrix between the  $k^{\text{th}}$  path between pair  $(i,j)$  and airlink  $(h,l)$ :  $a_{ij}^{khl} = 1$  if airlink  $(h,l)$  belongs to the  $k^{\text{th}}$  path between origin  $i$  and destination  $j$ , otherwise,  $a_{ij}^{khl} = 0$ ;

Here the total flown length is minimized (relation (2)) under capacity constraints (relation 3) for all the candidate elementary airlinks, constraint (4) insures that demands between pairs  $i, j$  are satisfied and constraints (5) recall the positive nature of the considered decision variables.

Then, if a solution is obtained, those links composing a used path (path  $k^*$  between  $i$  and  $j$  when  $x_{ij}^{k^*} > 0$ ) will be retained for proper equipment in the air logistic network. When no solution is available, constraints (3) can be relaxed to allow a limited number of multiple paths while demand must be assigned to several paths. This will be part of the flow management function of the Air Traffic Manager.

To produce acceptable solutions to the above linear network optimization problem, a greedy heuristic solution approach has been developed and its application to a medium size problem is considered.

The above formulation assumes that the  $K$  shortest paths problem has been solved for each pair of origin and destination. This can be performed using a generalization of Dijkstra's algorithm (Yen, 1971), while Yen's algorithm produces the  $K$  shortest loop less paths [14]. The complexity of such algorithms is polynomial, but in practice they lead to a very large amount of computation and memory space. Another limitation of this approach is that it is a static formulation whose solution does not provide hints for the management of the dynamic loading process of the network.

## Proposed heuristic solution approach

A different approach avoiding this calculation is developed here. The main ideas are to favor the most direct paths for each origin destination pair through a progressive loading of the network which can provide the dynamic routing policy of the Air Traffic network Management. The proposed approach is composed of the following steps:

- 0) Set  $\delta_{ij} = D_{ij} x_{ij} = 0 \forall i, j, i \in O, j \in D, L_{min} = 0$ , the initial decision space is the original network (the directed graph with its link capacities).
- 1) Use an algorithm such as Dijkstra's to compute the minimum paths between each origin and each destination with a nonzero demand in the current graph decision space. If there is no path between an origin and a destination, the corresponding demand for service  $\delta_{ij}$  cannot be fulfilled and must be deleted from the formulation. This residual demand could be processed through a ground transportation mode.
- 2) Compute the incidence matrix of the minimum path linking pair  $(i, j)$  and airlink  $(h,l)$ ,  $[a_{ij}^{1hl}]$ , as well as the length of each minimum path  $L_{ij}^1$  in the current decision space.
- 3) Assign the current demand  $[\delta_{ij}]$  to the minimum length paths between each origin and destination pair.
- 4) Compute for each origin  $i$  destination  $j$  pair and the load factor  $L_{ij}$  defined as follows:

$$L_{ij} = C_{hl} / (\sum_{\alpha \in O} \sum_{\beta \in D} a_{\alpha\beta}^{1hl} \delta_{\alpha\beta}) \quad (6)$$

- a. If  $L_{ij} \geq 1$  the current solution for the origin  $i$  destination  $j$  pair is given by:

$$x_{ij} = x_{ij} + \delta_{ij} \quad (7)$$

is feasible and the overall performance is updated by:

$$L_{min} = L_{min} + L_{ij}^1 \cdot \delta_{ij} \quad (8)$$

- b. If  $L_{ij} < 1$  that means that the capacities of some arcs in the current path between origin  $i$  and destination  $j$  are exceeded: only  $_{ij} \delta_{ij}$  is assigned to this path;
- 5) Coming back to the whole network:
- The newly saturated arcs  $(h, l)$  of the network such as  $\sum_{i \in O} \sum_{j \in D} a_{ij}^{1hl} \delta_{ij} = C_{h,l}$  are removed from the graph of the decision space;
  - The capacities of the remaining arcs are updated:

$$C_{h,l} \leftarrow C_{h,l} - \sum_{i \in O} \sum_{j \in D} a_{ij}^{1hl} \delta_{ij} \quad (9)$$

- The residual demand is computed for each origin destination pair:

$$\delta_{ij} \leftarrow \delta_{ij} (1 - \lambda_{ij}), \forall i, j, i \in O, j \in D \quad (10)$$

- 6) Go back to step 1.

Observe that the convergence of the algorithm towards a global or a partial (part of demand is deleted by the lack of a path between the corresponding origins and destinations) feasible solution is trivial. The algorithm ends when no residual demand remains. The computation burden, even for very large networks, is rather reduced since at each iteration the more demanding effort is to compute a minimum path for each residual demand over a reduced network without considering effectively the values of the remaining strictly positive capacities of the links.

## Illustration of the proposed approach

Figure 1 gives a scale representation of a considered network with two origins and four destinations, where the number associated to the twenty four two-ways links are the capacities.

Arcs with both extremities part of  $\{a, b, c, d, e, f\}$  have a capacity of 20, while all other arcs have a capacity of 40. Total demand is displayed in Table 1.

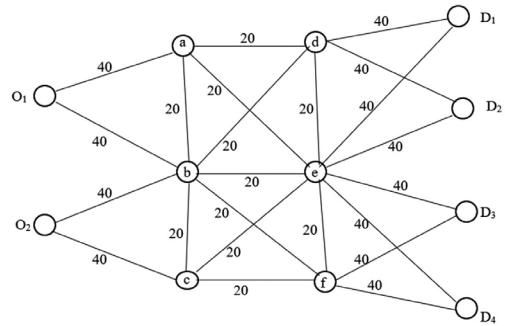


Figure 1. The considered logistic network

Table 1  
Distribution of initial demand

	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>
O <sub>1</sub>	10	20	20	10
O <sub>2</sub>	10	10	10	10

Observe that the min cut methods lead to a network capacity of 140, which is superior to 100, the total of demands. The first iteration of the algorithm provides the results displayed in Table 2 with the reduced available network of Figure 2.

Table 2  
First assignment of flows to paths

Shortest paths	Path flow	Length	$\lambda_{ij}$	$\chi_{ij}$	$\delta_{ij}$
O <sub>1</sub> -a-d-D <sub>1</sub>	10	3	2/3	20/3	10/3
O <sub>1</sub> -a-d-D <sub>2</sub>	20	3	2/3	40/3	20/3
O <sub>1</sub> -b-e-D <sub>3</sub>	20	4	2/3	40/3	20/3
O <sub>1</sub> -b-f-D <sub>4</sub>	10	4	2	10	0
O <sub>2</sub> -b-d-D <sub>1</sub>	10	4	1	10	0
O <sub>2</sub> -b-e-D <sub>2</sub>	10	3	2/3	20/3	10/3
O <sub>2</sub> -c-f-D <sub>3</sub>	10	3	1	10	0
O <sub>2</sub> -c-f-D <sub>4</sub>	10	4	1	10	0

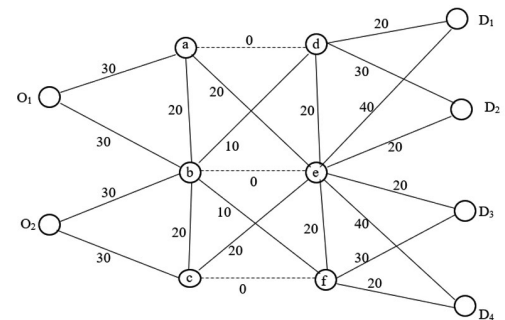


Figure 2. The reduced logistic network



The second iteration of the algorithm provides the results displayed in Table 3 with the residual network of Figure 3.

**Table 3.**  
Second assignment of flows to paths

Shortest paths	Path flow	Length	$\lambda_{ij}$	$X_{ij}$	$\delta_{ij}$
$O_1$ -b-d- $D_1$	10/3	5	3	10/3	0
$O_1$ -a-e- $D_2$	20/3	5	3/2	20/3	0
$O_1$ -a-e- $D_3$	20/3	5	3/2	20/3	0
$O_2$ -c-e- $D_2$	10/3	5	6	10/3	0

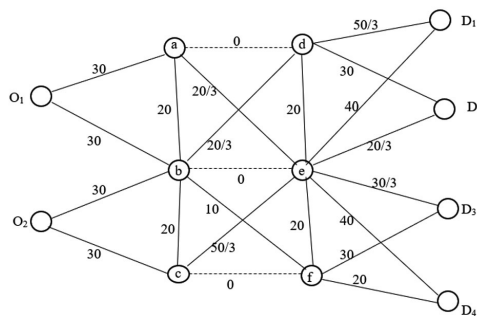


Figure 3. The final reduced logistic network

To the proposed solution corresponds a total round-trip distance of nine hundred with a mean distance of nine distributed over twelve different paths using a total of seventeen links over twenty-four. Observe the final reduced logistic network presents still a total flow capacity of 40.

A simple rule here to assign new incoming traffic in the logistic network during a considered period of time will be to distribute it among the generated paths proportionally to the computed flows provided by the proposed heuristic. For example, 2/3 of traffic between  $O_1$  and  $D_1$  will use path  $O_1$ -a-d- $D_2$  and 1/3 of traffic between  $O_1$  and  $D_1$  will use path  $O_1$ -b-d- $D_1$ .

## Conclusion

In this study, the prediction of the distribution of UAVs flows devoted to general logistics in the urban airspace has been considered. The objective has been to allow

more direct flights for the logistics operators, as well as to limit the impact of this traffic over the surrounding population. The limitation of this impact is effective by considering at the same time practical flow capacities for the candidate air links and by concentrating these flows in a reduced number of air links along minimum length paths between origin and destination pairs. The proposed heuristic strongly reduces the computational burden generally associated to flows assignment problems and allows to tackle very large-scale logistics networks. The quality of the solutions will depend on the accuracy of the prediction of demand between origins and destinations, as well as on the link capacity settings of the quality of the air. The implementation of the proposed solution is eased by the definition of the paths to be followed between each origin-destination pair and the distribution of traffic between these paths. Future work will extend this approach to consider more directly air traffic conflict limitations specially at intersections.

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